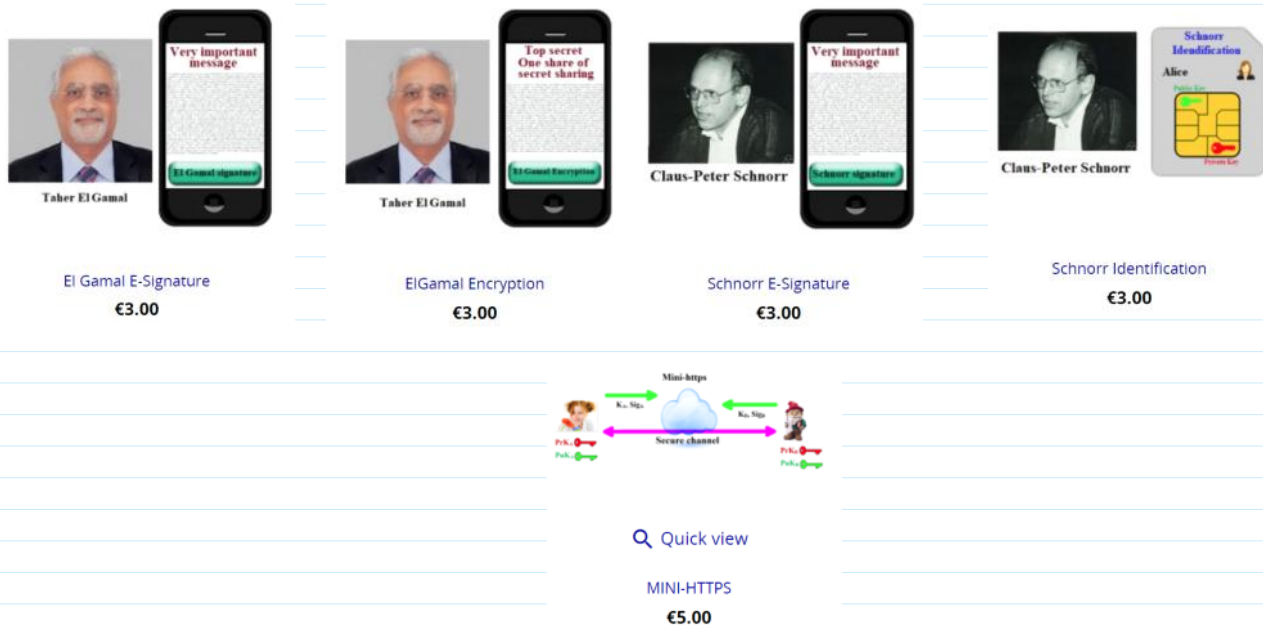


The problems to be solved during the final exam: contact participation.



Public Parameters **PP** = (**p**, **g**):

>> p=strongprime(28)

p = 268435019

g=2;

p - strong prime; **g** - generator.

>> p=int64(268435019)

p = 268435019

g=2;

Private key **PrK** and public key **PuK** generation for **Alice** and **Bob**.

PrK = **x** <- randi ==> **PuK** = **a** = **g**^{**x**} mod **p**

>> x=int64(randi(p-1))

x = 13426057

>> a=mod_exp(g,x,p)

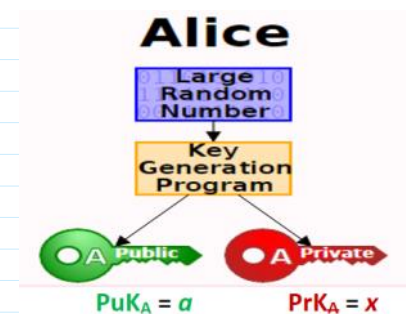
a = 2045067

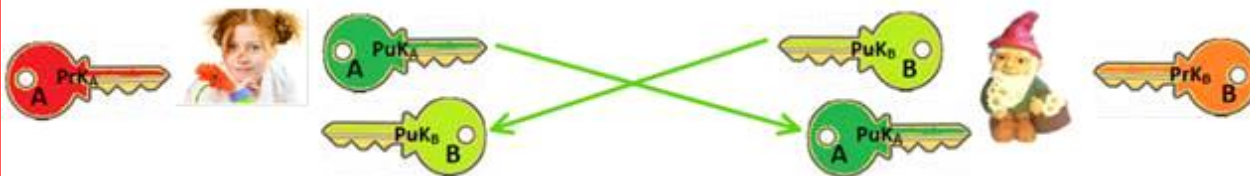
>> y=int64(randi(p-1))

y = 13426057

>> b=mod_exp(g,y,p)

b = 2045067





Public Key Infrastructure - PKI

Viešojo Rakto Infrastruktūra - VRI

Alice: (PrK_A, PuK_A)

Bob: (PrK_B, PuK_B)

$$PuK_A = \alpha = g^x \mod p$$

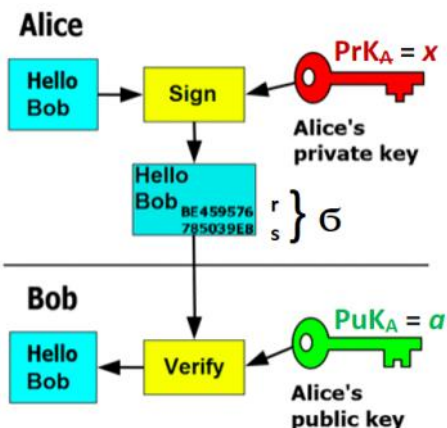
M message to be signed: Loan Contract.

$$|M| \sim 10 \text{ KB}$$

Hash and sign paradigm:

$$h = H(M); |h| \sim 256 \text{ bits} \leftarrow \text{SHA 256}$$

$$\text{Sign}(PrK_A, h) = \sigma = (r, s)$$



$$M, \sigma, PuK_A \rightarrow 1) h' = H(M')$$

$$2) \text{Ver}(PuK_A, \sigma, h') = \begin{cases} \text{True} \\ \text{False} \end{cases}$$

1) If $\text{Ver} = \text{True}$, then signature σ is formed using A's private key PrK_A which corresponds (is mathematically related) with A's public key PuK_A .

Lo: (PrK_z, PuK_z)

PuK_z

Impersonation

Dear Bob I am Lo and
I am sending you my
public key

Public Key Infrastructure - PKI

CA = (PrK_{CA}, PuK_{CA}) It is as notarius office

Certification Authority - CA \Rightarrow Registration Authorities - RA - subsidiaries of CA

Verisign
RA1 RA2 RA3 ----
<https://verysign.com>

Trusted Third Party - TTP \Rightarrow all users recognizes CA

PuK_{CA}
recognized by the user
browsers: Chrome, Opera...

$A: \text{PuK}_A \rightarrow RA \xrightarrow[\text{Data}_A]{\text{confirms } A, \text{identity } \text{PuK}_A}$

$CA: (\text{PrK}_{CA}, \text{PuK}_{CA})$
 $M_A = \text{PuK}_A \parallel \text{Data}_A$
 $h_A = H(\text{PuK}_A \parallel \text{Data}_A)$
 $\sigma_A = \text{Sign}(\text{PrK}_{CA}, h_A)$
 $\text{Cert}_A = \sigma_A \parallel \text{PuK}_A \parallel \text{Data}_A$

$A: \text{PuK}_{CA}.$
 $\xleftarrow{\text{Cert}_A, \text{PuK}_{CA}}$
 $h_A = H(\text{PuK}_A \parallel \text{Data}_A)$
 $\text{Ver}(\text{PuK}_{CA}, \sigma_A, h_A) = \begin{cases} \text{True} \\ \text{False} \end{cases}$

$\text{Sign}(\text{PrK}_A, h) = \sigma; M, \sigma, \text{PuK}_A \xrightarrow{\text{Cert}_A} B: \text{PuK}_{CA}, \text{PuK}_A$
 1) $\text{Cert}_A \xrightarrow{M, \sigma} \sigma_A \parallel \text{PuK}_A \parallel \text{Data}_A$
 2) $h''_A = H(\text{PuK}_A \parallel \text{Data}_A)$
 3) $\text{Ver}(\text{PuK}_{CA}, \sigma_A, h''_A) = \begin{cases} \text{True} \\ \text{False} \end{cases}$
 4) $h' = H(M)$
 5) $\text{Ver}(\text{PuK}_A, \sigma, h') = \begin{cases} \text{True} \\ \text{False} \end{cases}$

X509 v3 Standard

SerialNumber

Issuer } Verisign

notBefore } 2021.11.10; 18:10:07

notAfter } 2022.11.10; 18:10:07

Subject } A

Algorithm } ECDSA

SubjectPublicKey } PuK_A

extensions

$Lo \leftarrow \text{Cert}_Z \leftarrow CA$

2021.11.12; 19:10:11

2022.11.12; 19:10:11

2022.11.12; 19:10:12

$Lo: (\text{PrK}_Z, \text{PuK}_Z); \text{Cert}_Z.$

L - loan contract $\rightarrow h = H(L)$

$\text{Sign}(\text{PrK}_Z, h) = \sigma_Z$

$L, \sigma_Z, \text{PuK}_Z \xrightarrow{\text{Cert}_Z} B: \begin{matrix} 1) + \\ 2) + \\ 3) + \\ 4) + \end{matrix}$
 $\xleftarrow{\text{Money}}$

Cert_2 2) +
 Money 3) +
 ← transfer 4) +
 ← to pay % for 5) +
 the loan
 sorry my loan contract
 is invalid since

at the time you've signed it my certificate validity term expired

CA services: CRL - Certificates Revocation List

OCSP - On-line Certificates Status Protocol

6) Verify if Cert_2 is not in certification revocation list (CRL).

7) If validity of Cert_2 is not expired.

• Certificates Revocation List - CRL:

Is a list of [digital certificates](#) that have been revoked by the issuing [certificate authority](#) (CA) before their scheduled expiration date and should no longer be trusted.

There are two different states of revocation defined in RFC 5280:

Revoked

A certificate is irreversibly revoked if, for example, it is discovered that the certificate authority (CA) had improperly issued a certificate, or if a private-key is thought to have been compromised. Certificates may also be revoked for failure of the identified entity to adhere to policy requirements, such as publication of false documents, misrepresentation of software behaviour, or violation of any other policy specified by the CA operator or its customer. The most common reason for revocation is the user no longer being in sole possession of the private key (e.g., the token containing the private key has been lost or stolen).

Hold

This reversible status can be used to note the temporary invalidity of the certificate (e.g., if the user is unsure if the private key has been lost). If, in this example, the private key was found and nobody had access to it, the status could be reinstated, and the certificate is valid again, thus removing the certificate from future CRLs.

A CRL is generated and published periodically, **often at a defined interval**. A CRL can also be published immediately after a certificate has been revoked. A CRL is issued by a CRL issuer, which is typically the CA which also issued the corresponding certificates, but could alternatively be some other trusted authority. All CRLs have a lifetime during which they are valid; this timeframe is often **24 hours or less**. During a CRL's validity period, it may be consulted by a PKI-enabled application to verify a certificate prior to use.

To prevent [spoofing](#) or [denial-of-service attacks](#), CRLs usually carry a [digital signature](#) associated with the CA by which they are published. To validate a specific CRL prior to relying on it, the certificate of its corresponding CA is needed.

The certificates for which a CRL should be maintained are often [X.509/public key certificates](#), as this format is commonly used by PKI schemes.

From <https://en.wikipedia.org/wiki/Certificate_revocation_list>

• On-line Certificates Status Protocol - OCSP:

Is an [Internet protocol](#) used for obtaining the revocation status of an [X.509 digital certificate](#).^[1] It is described in RFC 6960 and is on the [Internet standards](#) track. It was created as an alternative to [certificate revocation lists](#) (CRL), specifically addressing certain problems associated with using CRLs in a [public key infrastructure](#) (PKI).^[2] Messages communicated via

OCSP are encoded in [ASN.1](#) and are usually communicated over [HTTP](#). The "request/response" nature of these messages leads to OCSP [servers](#) being termed *OCSP responders*.

Some [web browsers](#) use OCSP to validate [HTTPS](#) certificates.

- Since an OCSP response contains less data than a typical certificate [revocation list](#) (CRL), it puts less burden on network and client resources. [\[3\]](#)
- Since an OCSP response has less data to [parse](#), the client-side [libraries](#) that handle it can be less complex than those that handle CRLs. [\[4\]](#)
- OCSP discloses to the responder that a particular network host used a particular certificate at a particular time. OCSP does not mandate encryption, so other parties may intercept this information. [\[1\]](#)

From <https://en.wikipedia.org/wiki/Online_Certificate_Status_Protocol>

Qualified and Non-qualified certificates

mathes with e-signature law
Is valid according to contract between parties

Eureka
EU e-document system
2008 m. - 2009 m.
Gcomalto Sagem
800 000 € 1200 000 € ...
Σ ~ 2 400 000

Time Stamping Authority - TSA - Trusted Third Party (TTP)

A: L - loan contract $\rightarrow h = H(L)$

$\text{Sign}(\text{PrK}_A, h) = \sigma$ $\xrightarrow[\text{Cert}_A]{L, \sigma, \text{PrK}_A}$ TSA: $(\text{PrK}_{TS}, \text{PrK}_{TS}), \text{Cert}_{TS}.$
 $\text{PrK}_{CA}, \text{PrK}_A \quad h \approx H(L)$

1. $\text{Ver}(\text{PrK}_{CA}, \text{Cert}_A) = \text{True}$
2. $\text{Ver}(\text{PrK}_A, \sigma, h) = \text{True}$
3. $DT = \text{YYYY.MM.DD:hh:mm:ss:...}$
4. $h_{TS} = H(h, \sigma, DT, \text{PrK}_{TS}, \text{Cert}_{TS})$

A: PrK_{CA}

1. Verifies DT

2. Verifies validity of Cert_{TS}

3. $h'_{TS} = H(h, \sigma, DT, \text{PrK}_{TS}, \text{Cert}_{TS})$

4. $\text{Ver}(\text{PrK}_{TS}, \sigma_{TS}, h'_{TS}) = \text{True} \Rightarrow \text{It: } \left\{ \begin{array}{l} h'_{TS} = h_{TS} \\ \text{PrK}_{TS} = \text{PrK}_{TS} \end{array} \right\} \rightarrow \text{True}$

$$4. \text{Ver}(\text{Puk}_{TS}, \tilde{\sigma}_{TS}, h'_{TS}) = \text{True} \Rightarrow \text{It: } \left\{ \begin{array}{l} h'_{TS} = h_{TS} \\ \text{Puk}_{TS} = g^{x_{TS}} \bmod p \end{array} \right\} \rightarrow \text{True}$$

$$L' = L \parallel \text{DT} \parallel \tilde{\sigma}_{TS}$$

$$h_L = H(L')$$

$$\tilde{\sigma}_L = \text{Sign}(\text{PrK}_A, h_L) = \tilde{\sigma}_L$$

A:

$$L', \tilde{\sigma}_L, \text{Puk}_A, \text{Cert}_A \rightarrow$$

$$\text{DT}, \tilde{\sigma}_{TS}, \text{Puk}_{TS}, \text{Cert}_{TS}$$

$$B: (\text{PrK}_B, \text{Puk}_B); \text{Puk}_{CA}$$

$$1. \text{Ver}(\text{Puk}_{CA}, \text{Cert}_{TS}) = \text{True}$$

$$2. \text{Ver}(\text{Puk}_{CA}, \text{Cert}_A) = \text{True}$$

$$3. h_L = H(L'); \quad h_{TS} = H(h, \tilde{\sigma}, \text{DT}, \text{Puk}_{TS}, \text{Cert}_{TS})$$

$$4. \text{Ver}(\text{Puk}_{TS}, \tilde{\sigma}_{TS}, h_{TS}) = \text{True}$$

$$5. \text{Ver}(\text{Puk}_A, \tilde{\sigma}_L, h_L) = \text{True}$$

6. OCSP: to verify that certificates are in the interval:

[notBefore, notAfter] \rightarrow Yes

7. CRL: do the Cert_A and Cert_{TS} not revoked \rightarrow No

A:

\leftarrow money transfer \mathcal{B}